

# 121/1 MATHEMATICS-Alt.A Paper 1 Sept. 2024 - $2\frac{1}{2}$ hours TRIAL EXAMINATION-2024

Name:	Index Number:				
Student's Signature:	Date:	ADM NO			

## Instructions to candidates

- (a) Write your name and index number in the spaces provided above.
- (b) Sign and write the date of examination in the spaces provided above.
- (c) This paper consists of two sections: Section I and Section II.
- (d) Answer all questions in Section I and only five questions in Section II.
- (e) Show all the steps in your calculations, giving your answers at each stage in the spaces provided below each question.
- (f) Marks may be given for correct working even if the answer is wrong.
- (g) Non-programmable silent electronic calculators and KNEC Mathematical tables may be used except where stated otherwise.
- (h) This paper consists of 15 printed pages.
- (i) Candidates should check the question paper to ascertain that all the pages are printed as indicated and that no questions are missing.
- (j) Candidates should answer the questions in English.

#### For Examiner's Use Only

## Section I

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	Total

#### Section II

17	18	19	20	21	22	23	24	Total



Answer **all** the questions in this section in the spaces provided.

1. Evaluate without using a calculator; 
$$\frac{\frac{1}{3} \times \frac{4}{7}}{0.2} - \frac{\frac{2}{9} \div (-4^2)}{0.5}$$
 (3 marks)

2. Find the values of x which satisfy the equation;  $3^{2x} - 4 \times 3^x + 3 = 0$  (4 marks)

3. Under an enlargement of scale factor 3 a point A(1, 2) is mapped onto A'(13, 8). Find the centre of enlargement by calculation. (3 marks)

4. Given that  $sin (5\theta)^{\circ} = cos(4\theta)^{\circ}$ , find  $tan(3\theta - 8)^{\circ}$  giving your answer to 4 significant figures. (3 marks) 5. A flag post 12m long is fixed on top of a tower. From a point on a horizontal ground, the angles of elevation of the top and bottom of the flag post are 46° and 33° respectively. Calculate the horizontal distance from the point on the ground to the foot of the tower. (4 marks)

6. The diagram shows a sketch of a curve  $y = x^2 - 3x + 6$  intersecting with the line y = 10 for  $-1 \le x \le 4$  at points Aand B.



(a) Complete the table below for *the function*  $y = x^2 - 3x + 6$  (1 mark)

Х	-1	0	1	2	3	4
v						

(b) Using trapezium rule with 6 ordinates, estimate the area bounded by the curve  $y = x^2 - 3x + 6$  and the line y = 10. (3 marks)

7. A carpenter has three wooden bars measuring 10.5 m, 12.6 m and 14.7 m. He cuts the bars into pieces of equal lengths. Calculate the least number of pieces obtained. (3 marks)

8. In the diagram below, ABCD is a trapezium with AB parallel to DC. The perpendicular distance between AB and DC is 5cm. The area of the trapezium is 40cm<sup>2</sup> and the ratio between AB:DC=3:2.





(2 marks)

9. Simplify the following expression; 
$$\frac{p^2 - 2ap - 2a + p}{(p+1)(2a^2 - ap)}$$
 (3 marks)

10. In the figure below, O is the centre of the circle. AC=6cm, BC=9cm and angle  $ACB=132^{\circ}$ 



(a) Calculate the length of AB correct to 2 decimal places. (2 marks)

11. Given 
$$\mathbf{A} = \begin{pmatrix} 1 & 3 \\ 2 & 0 \end{pmatrix}$$
 and  $\mathbf{B} = \begin{pmatrix} 4 & 2 \\ 1 & 5 \end{pmatrix}$ , find the determinant of  $\mathbf{A}^2 - \mathbf{B}$ . (3 marks)

12. John bought a cooker at Ksh. 27 000 after being allowed a discount of 10%. Calculate the marked price of the cooker. (2 marks)

13. A pice of wire 20cm long is bent into the shape of a rectangle. Find the maximum area it encloses. (3 marks)

14. Using a ruler and a pair of compasses only, construct;(a) A rhombus ABCD in which AC=10cm and angle BAD = 60°.

(3 marks)

(b) A perpendicular from X , the point of intersection of the two diagonals of the rhombus in 14(a) above to meet AB at N. Measure XN. (1 mark)

15. The length of a rectangular floor of a room is 4m longer than the width. If the area of the floor is  $96m^2$ , find the perimeter of the floor of the room. (3 marks)

16. The figure below shows a histogram of a certain set of data obtained from mathematics test.



Draw a vertical line, in the histogram, showing where the median mark lies. Hence estimate the median mark. (3 marks)

## **SECTION II (50 marks)**

Answer only **five** questions from this section in the spaces provided.

17. The diagram below shows the speed – time graph for a bus travelling between two stations. The bus begins from rest and accelerates uniformly for 30 seconds. It then travelled at a constant speed for 60 seconds and finally decelerates uniformly for 40 seconds.



(d) The time the bus takes to travel the first half of the journey. (3 m	narks)
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18. The table below shows the frequency distribution of heights of plants in a tree nursery.

H	eights(cm)	0-10	10-20	20-30	30-40	40-50	50-60
N	umber of plants	4	8	10	k	4	2

The mean height of the plants is 27.5cm.

(a) Determine the value of k.

(4 marks)

(b) \$	State;
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(i)	The modal class.	(1 mark)

(ii) The modal frequency. (1 mark)

(c) Calculate the median height of the plants correct to 4 significant figures. (4 marks)

- 19. Four towns A,B,C and D are such that B is 70km from A on a bearing of 063°. C is 83km and on a bearing of S30°*E* from B. D is directly to the west of C and on a bearing of 161° from A. Using a scale of 1cm represent 10km;
  - (a) Show the relative positions of the towns.

(4 marks)

(b) From the diagram, find;

(i) The distance AC

(ii) The bearing of A from C

(2marks)

(1mark)

(c) An express train left town A at 12noon for town D via town B and C. If it arrived at town D at exactly 3.30pm on the same day, calculate the average speed of the train in km/hr. (3 marks)

- 20. The position vectors of points A and B are  $\binom{-1}{8}$  and  $\binom{9}{-2}$  respectively.
- (a) Determine;
  - i The magnitude of AB correct to **two** decimal places.

(3 marks)

ii The coordinates of M, the mid-point of AB.

(2 marks)

(b) A translation vector T maps the point M onto M<sup>1</sup>(3,5). Find the coordinates of A under the translation vector T. (3 marks)

(c) A point R is on OM produced such that  $2\overrightarrow{OR} = 5\overrightarrow{OM}$ . Find the column vector  $\overrightarrow{AR}$ . (2 marks)

- 21. A solid frustrum of cone is such that the radii of the bottom and top circular faces are 5cm and 1.5cm respectively. The slant height of the frustrum is 7cm. (Use  $\pi = 3.142$ ) Determine correct to **two** decimal places;
  - (a) The height of the frustrum.

(2 marks)

(b) The volume of the frustrum.

(4 marks)

(c) The surface area of the frustrum.

(4 marks)

- 22. A triangle PQR is such that angle QPR=90°. The vertices of the triangle are P(2,4), Q(10,8) and R(m, n). The equation of line QR is 2x + 11y = 108.
  - (a) Determine:
    - (i) The equation of line PR in the form ax + by + c = 0 where *a*, *b* and *c* are integers. (4 marks)

(ii) The coordinates of point R.

(3 marks)

(b) A straight line passes through point P and is parallel to line QR. Determine the x-intercept of the line. (3 marks)

- 23. The vertices of a triangle ABC are A(-1,-2), B(1,-5) and C(2,-1). Triangle A'B'C' is the image of triangle ABC under a reflection in the line x + y = 3.
  - (a) Draw triangles ABC and A'B'C' on the grid provided below.

(3 marks)



- (b) Draw triangle A"B"C"the image of A'B'C'under a rotation of +90° about centre (0,0) (2marks)
- (c) Draw triangle A'''B'''C''' the image of A''B''C''under an enlargement whose scale factor is -1 about centre (1, 2). State the coordinates of the image A'''B'''C''' . (3 marks)
- (d) State a pair of triangles which are:
  - i. Directly congruent;
  - ii. Oppositely congruent.

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(1mark)

(1mark)

(5 marks)

- 24. The equation of a curve is given by  $y = 2x^3 21x^2 + 36x 15$ .
  - (a) Determine the stationary points of the curve and state their nature.

(b) Determine;

(i) The equation of a tangent to the curve at a point where x = 2 (3 marks)

(ii) The equation of a normal to the curve at a point where x = 2 (2 marks)

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